

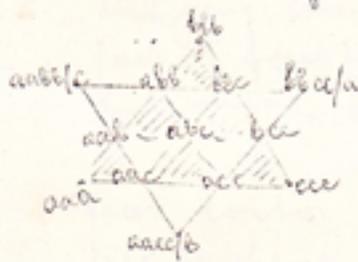
October 1st 1970

Dear doctor Wilson

These last weeks I have been playing with combining musical systems. Perhaps you might be interested in it, and therefore I have pleasure to communicate with you. The element of a system is chosen to be a chord of three notes, having intervals a/b, b/c and c/a, and you can write it as a triangle



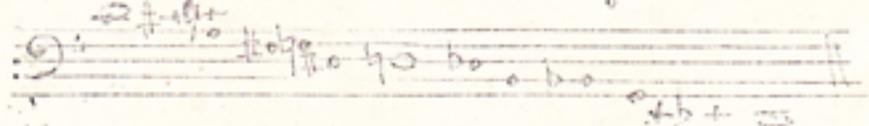
We can multiply these numbers at pleasure, and write the chord $\begin{matrix} b \\ abc \end{matrix}$. I choose the number abc as the



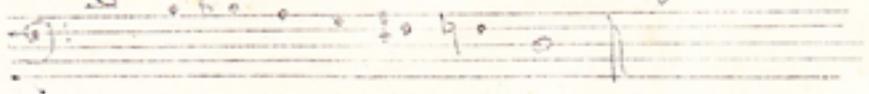
the centre of my system: and I surround it by triangles, representing either the same chords, with $a:b:c$, or the inverse ones with $1/a:1/b:1/c$.

You see what I mean. There are thirteen notes in all. You may leave out the central one, and

have a scale of ~~thirteen~~ twelve notes, or you may leave out the six outmost notes, and have a scale of seven notes. Even with the cold classical numbers 4, 5, 6 you get a scale not known in classical music. For instance, choosing a as central note



This includes a coherent scale of seven notes only



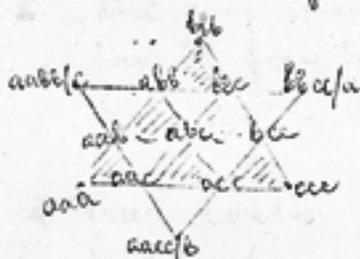
October 1st 1970

Dear doctor Wilson

These last weeks I have been playing with combining musical systems. Perhaps you might be interested in it, and therefore I have pleasure to communicate with you. The element of a system is chosen to be a chord of three notes, having intervals a/b, b/c and c/a, and you can write it as a triangle



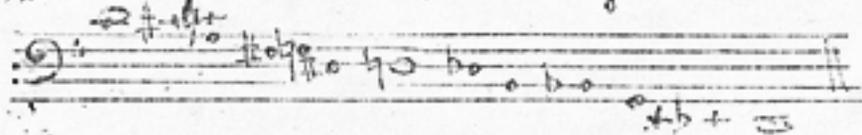
We can multiply these numbers at pleasure, and write the chord $\frac{bbc}{abc}$. I choose the number abc as the centre of my system: and I surround it



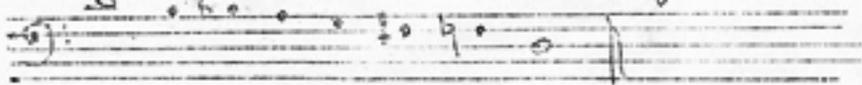
by triangles, representing either the same chords, with $a:b:c$, or the inverse ones with $1/a:1/b:1/c$.

You see what I mean. There are thirteen notes in all. You may leave out the central one, and

have a scale of ~~thirteen~~ twelve notes, or you may leave out the six outmost notes, and have a scale of seven notes. Even with the odd classical numbers 4, 5, 6 you get a scale not known in classical music. For instance, choosing d as central note



This includes a coherent scale of seven notes only



I leave to you the pleasure of finding the results resulting from the numbers $[5, 6, 7]$, and other ones.

In fact the results are the same which I gave in my book *Neue Musik mit 31 Tönen*, under the name *Kreispaarungen eines Dreiklangs*, mirroring cycles. Here the system has been represented in a diagram, like a "mandala". Last year you sent me your mandalas. I am so very sorry I have lost them, unfortunately. If you would kindly send me another set of them, I would be very grateful.

C. G. Jung, when writing on mandala, stresses the fact of fourfold symmetry. Your mandalas, and mine, use other numbers.

Dear doctor Wilson, I shall very much like to hear from you again.
With best wishes

Sincerely yours

A. D. Fowler

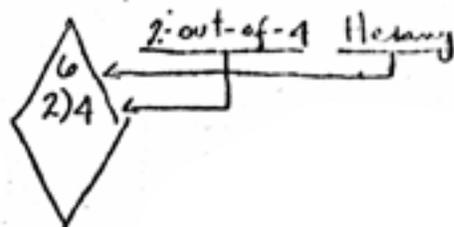
is a minimal symmetrical elaboration about the tetradic diamond.* I make no attempt to treat the diamonds as combinational sets. However, they are complementary to the combinational sets in the same way a \perp is complementary to a \square in a cross-hatched grid  etc.

The combinational sets (which I leave ~~at~~ suffixes like "-any") are intertice-centered, and do not imply a musical style tonically oriented to the tonic. The combinational sets, like the diamonds, give circular, "spherical", or "hyper-spherical" patterns. However, these are not universally self-mirroring. The self-mirroring sets are, in fact, restricted to the series, (1-out-of-2), 2-out-of-4, 3-out-of-6, 4-out-of-8, etc. I abbreviate these figures, and label them thus; 2)4 hexany, 3)6 eikozany, 4)8 hebdomekontany. It is these figures which are of exceptional interest to me.

* (The figure I label "Mandala" is an elaboration upon the 2)4 Hexany. 4 tetrads plus their 4 reciprocal tetrads flank the 8 facets of the Hexany. The hexany, itself, implies the number 4, as it is formed by combination of 2-out-of-4.)

No. of Tones	Name of combination set	(Primary molecule)
1	Monany	Monad
2	Dyanany	Dyad
3	Triany	Triad
4	Tetranany	Tetrad
5	Pentanany	Pentad
6	Hexany	Hexad
7	Heptany	Heptad
8	Oktonany	Oktoad
10	Dekany	
15	Pentadekany	
20	Eikosany	
21	Eikozimonany	
28	Eikozioctany	
35	Triakontapantany	
56	Pentakontahexany	
70	Heptakontany	

Examples:



I use Pascal's Triangle to codify the combination sets. I extend the meaning of the word "combination" to include 0-out-of-N, 1-out-of-N etc to N-out-of-N.

(OVER)

A. Each combinational-set contains the combinational-sets above it. Examples: The $2)4$ hexany contains the $1)3$ triany and the $2)3$ Triany, and consequently, the $0)2$ monany, the $1)2$ dyany, & the $2)2$ monany; and as the next consequence, the $0)1$ monany & the $1)1$ monany; and as a final consequence the $0)0$ monany.

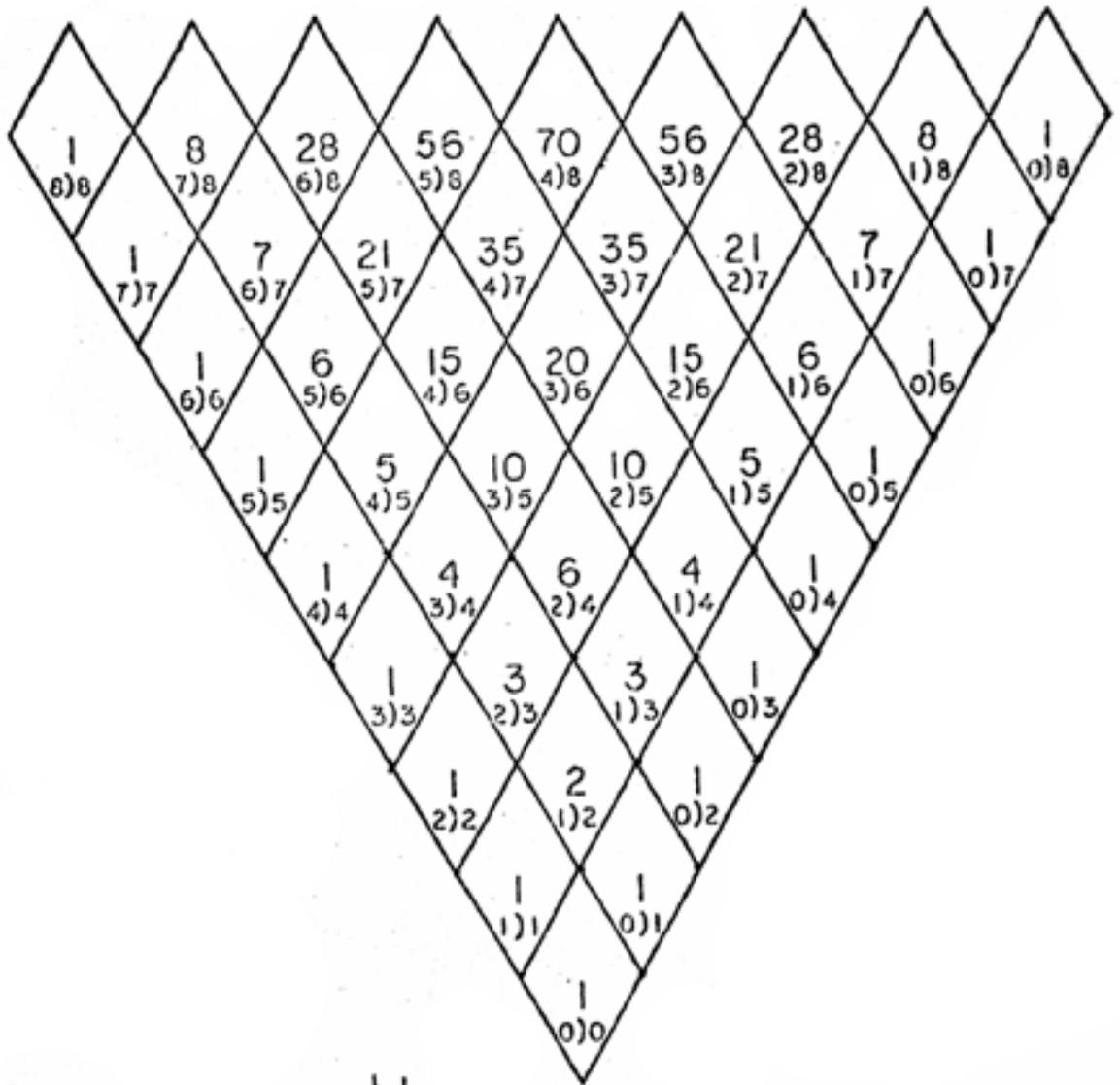
B. Each of the combinational sets derived from a given primary module may be said to ^{belong to} the (horizontal) order of tone-space identified by that module (Tetradic tone-space derives from tetrad etc) Each of the combination sets in a given order of tone-space, when taken as a subset of a given (applicable) "Matrix" set (in a higher order of tone-space) will variegate into a spectrum of varieties. Each of the combinations in a given order of tone-space will variegate into the same number of varieties in regards to the given matrix combination-set within which it occurs.

C. The number of such varieties (according to B) can be found by relating the order of tone-space (in which the combination occurs), in a descending vertical sequence to the numbers, in sequence, along the base of the Triangle formed by that order of tone-space containing containing the matrix combination-set,

Example in the $2)4$ hexany matrix:

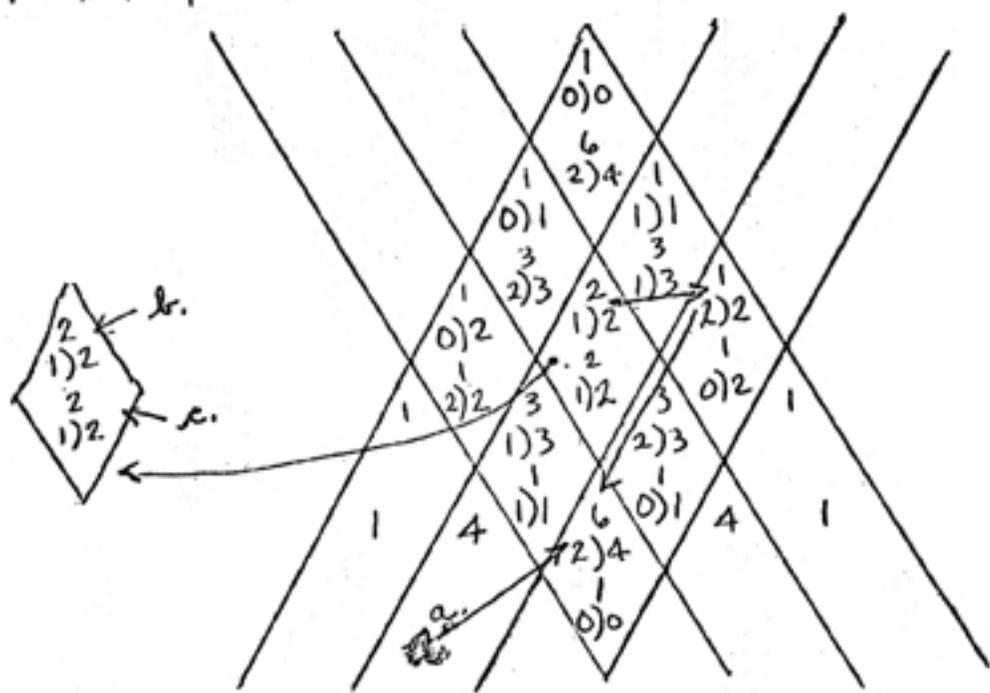
The zeroadic combination,	$0)0$ monany	has 1 variety
The monadic combinations,	$0)1$ monany & $1)1$ monany	have 4 varieties
The dyadic combinations,	$0)2$ monany $1)2$ dyany $2)2$ monany	have 6 varieties
The triadic combinations,	$1)3$ Triany & $2)3$ Triany	have 4 varieties
The Tetradic combination,	$2)4$ hexany	has 1 variety

Pascal's Triangle, Inverted



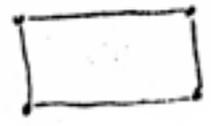
if I superimpose this ^{Inverted} triangle over the upright triangle in such a way that the nadir of the inverted triangle corresponds with a given combinational-set of the upright triangle, the overlapping area of the two triangles will give the sub-combinational-sets of said given combinational-set, (See example on another sheet)

D. Each of said varieties of the sub-set (according to BAC) will have a certain number of occurrences within the context of the matrix set. Each number of occurrences will form a combinational-cross-set to the ^{set}sub-set being considered. The number of occurrences, and combinational-cross-set which these form, may be located by generating an inverted Triangle (rotated 180° rather than mirrored) from the matrix set. Example for 2)4 hexany matrix:

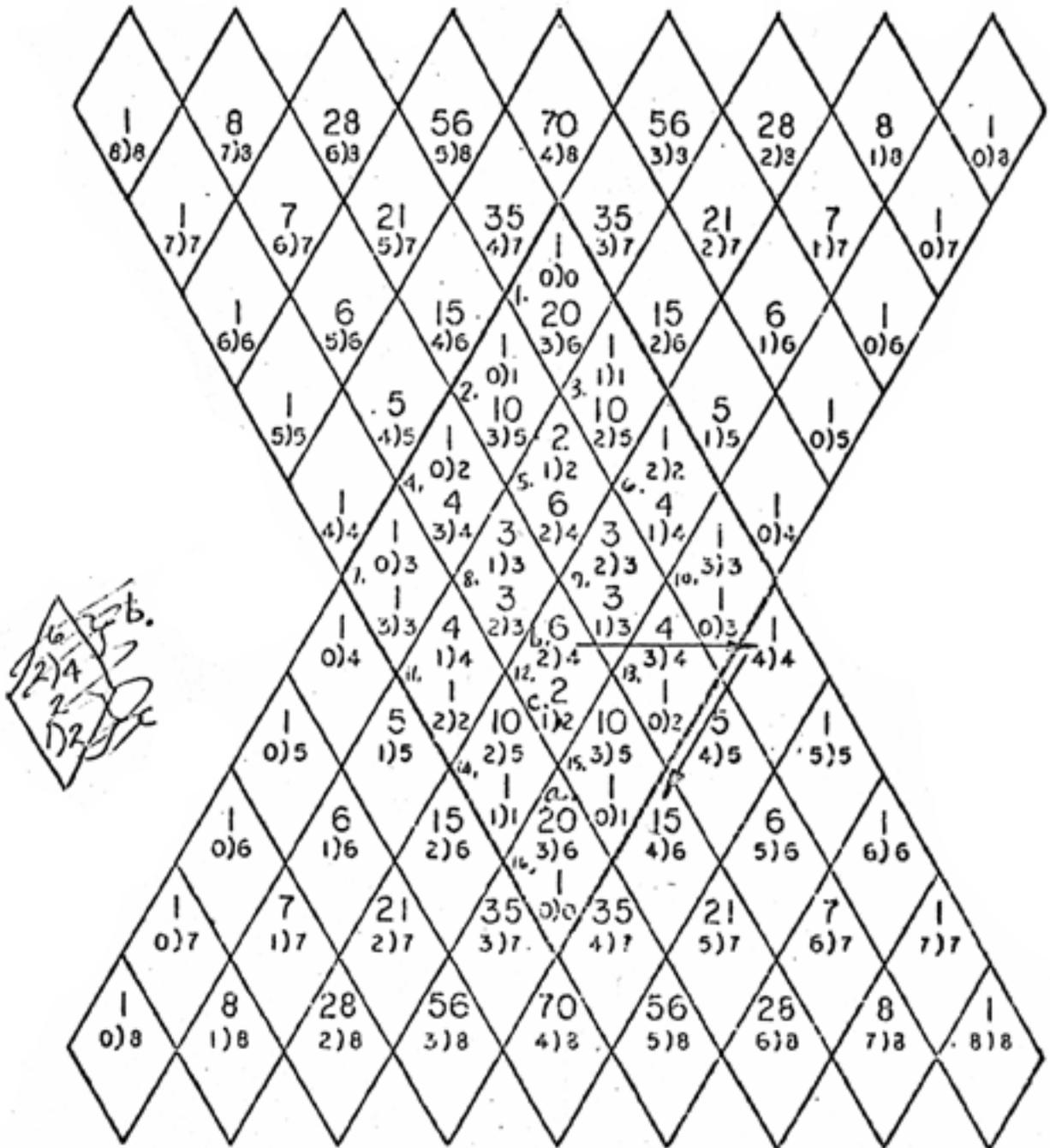


Thus, in the 2)4 hexany matrix (a.) the 1)2 dyadic sub-set (b.) has 6 varieties [green arrows] according to statement (c) each of which occurs 2. times in a 1)2 dyadic cross-set (c.)

The cross-set of the green dyadics is the orange dyadics:



Superimposition of the Inverted Triangle & Upright Triangle with the nadir of the inverted Triangle corresponding to the 3)6 Eikosany of the upright Triangle. (3)

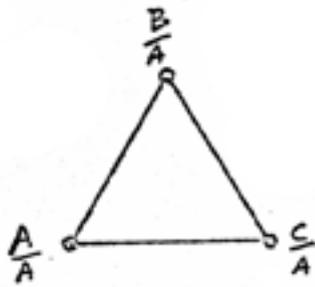


Example: In the 3)6 Eikosany Matrix (a.) the 2)4 hexany subset (b.) has 15 varieties (arrow) each of which occurs 2 times in a 1)2 dyany cross-set (c.). See other side of sheet for complete list of subsets.

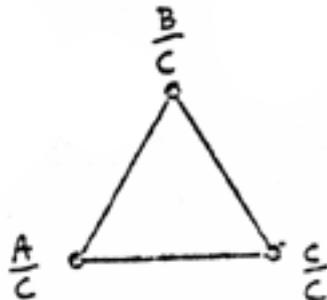
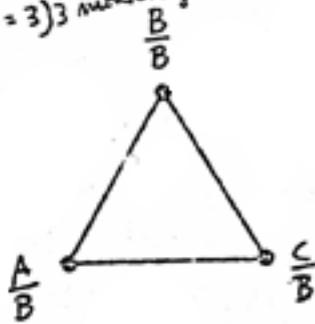
3)6 Eikosony Matrix :

Thombus No. and	Subset	Varieties of Subset	No. of occurrences each Variety	Cross-set
1.	0)0 Monony	1	20	3)6 Eikosony
2.	0)1 Monony	6	10	3)5 Dekany
3.	1)1 Monony	6	10	2)5 Dekany
4.	0)2 Monony	15	4	3)4 Tetrany
5.	1)2 Dyany	15	6	2)4 Hexany *
6.	2)2 Monony	15	4	1)4 Tetrany
7.	0)3 Monony	20	1	3)3 Monony
8.	1)3 Triany	20	3	2)3 Triany *
9.	2)3 Triany	20	3	1)3 Triany
10.	3)3 Monony	20	1	0)3 Monony
11.	1)4 Tetrany	15	1	2)2 Monony
12.	2)4 Hexany	15	2	1)2 Dyany
13.	3)4 Tetrany	15	1	0)2 Monony
14.	2)5 Dekany	6	1	1)1 Monony
15.	3)5 Dekany	6	1	0)1 Monony
16.	3)6 Eikosony	1	1	0)0 Monony

TRIAD

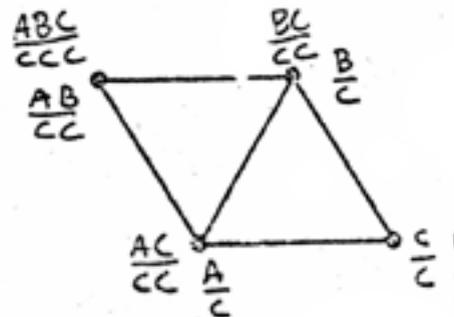
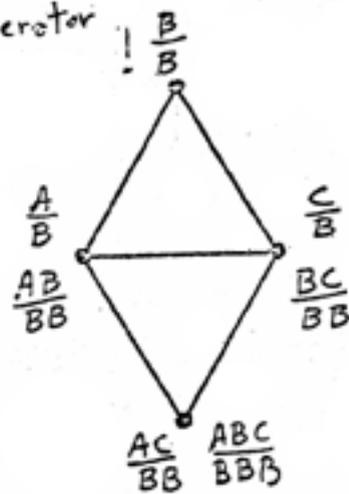
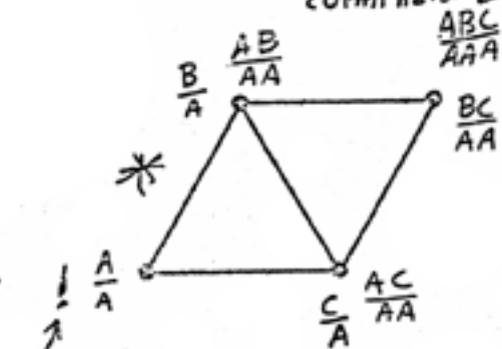


Gold = 0) 3 money
 Silver = 1) 3 money
 Red = 2) 3 money
 Purple = 3) 3 money

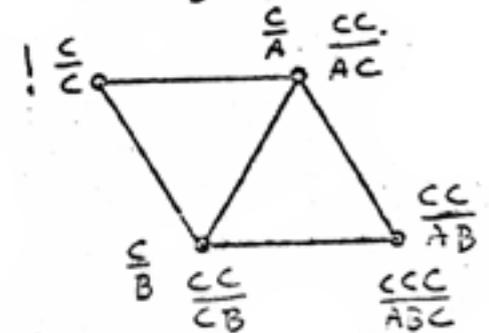
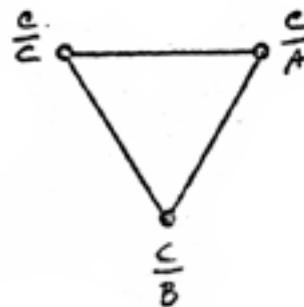
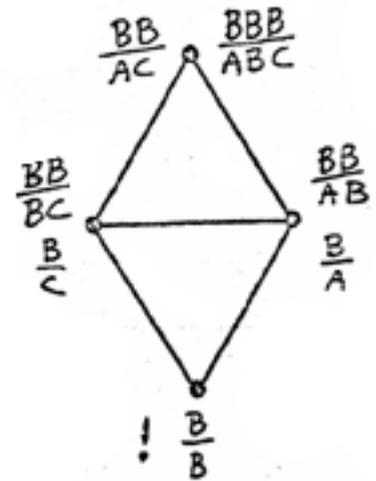
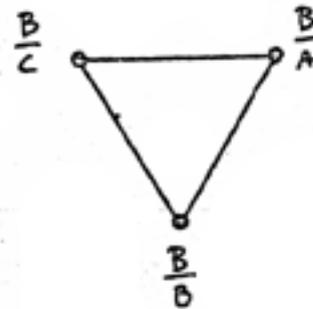
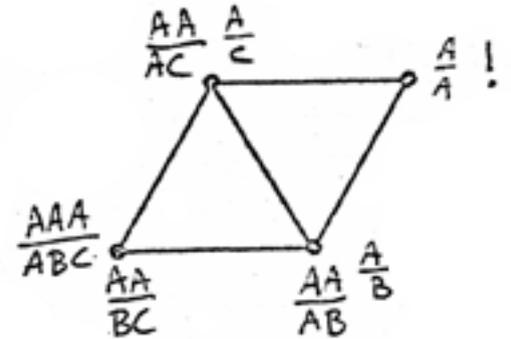
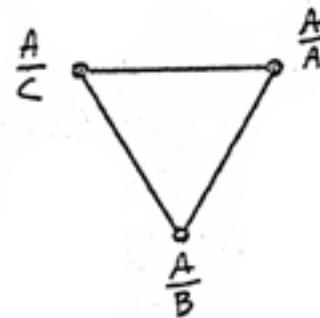


TRIADIC COMBINATIONAL SERIES'

culminator 2



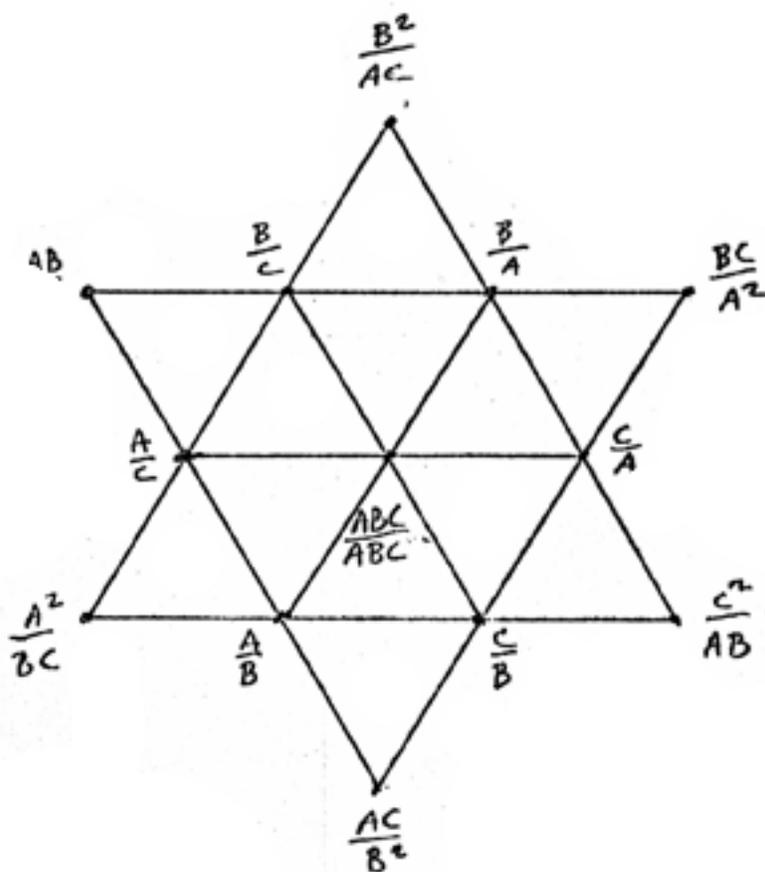
RECIPROALS



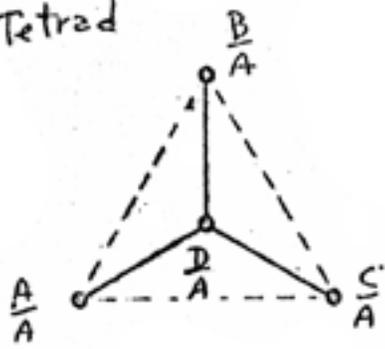
(OVER)

* If, in the asterisked figure, I assign to A, B, C values of 1, 3, 5. The resultant figure is identical to Euler's 13.5 genus, the generator being identical to his fundamental, and the culminator to his guiding-tone. However the remaining variations of the combinational series are significantly different from the Euler genus.

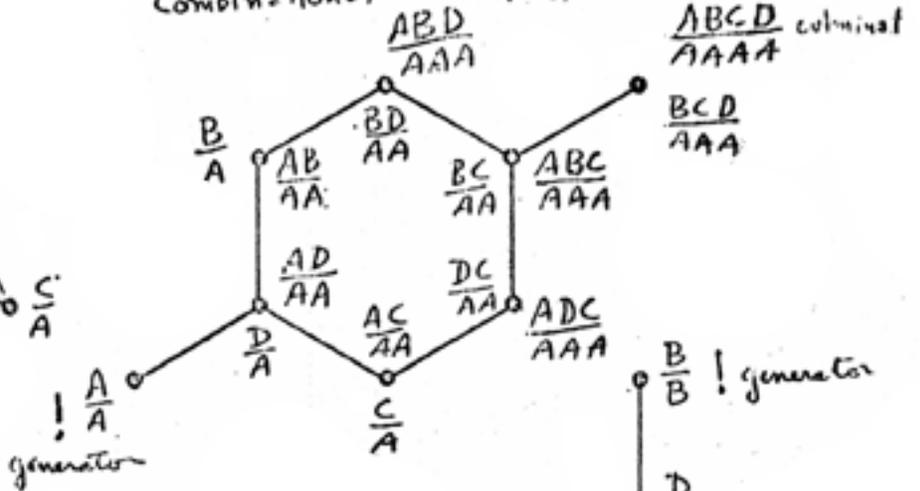
If I form a 6-fold aggregate of the tridic combinational series I arrive at your mirroring cycle.



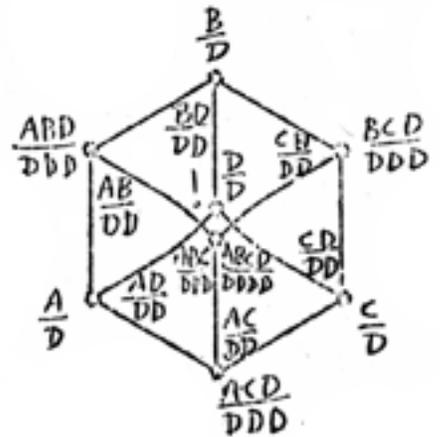
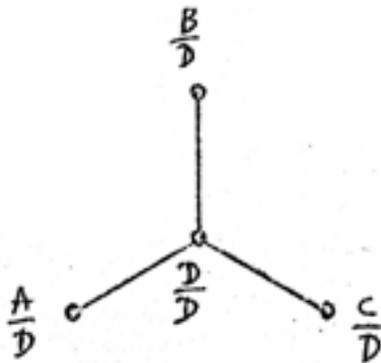
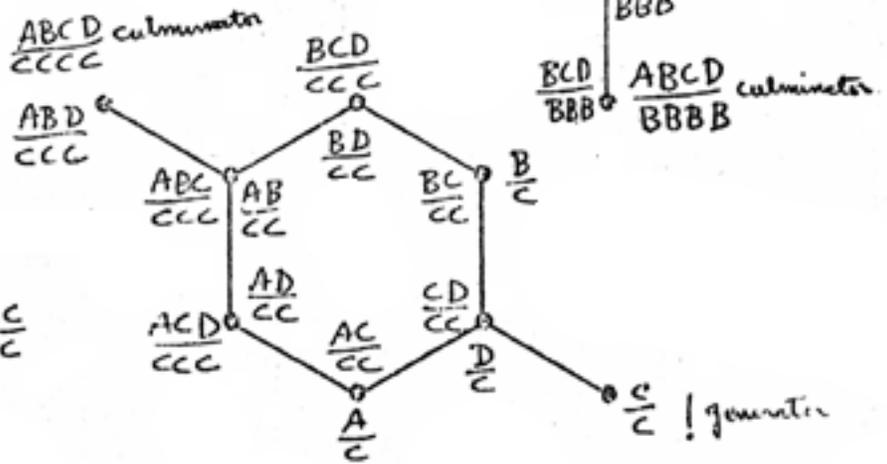
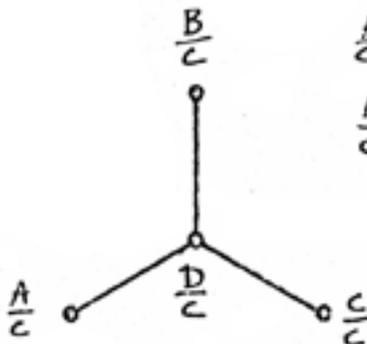
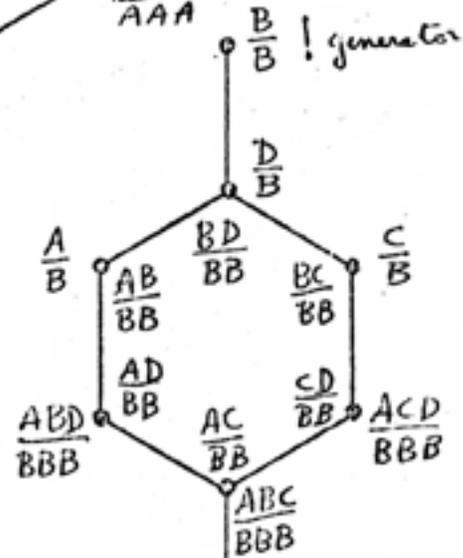
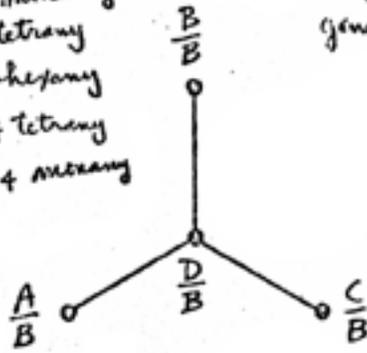
Tetrad



Combinational Series



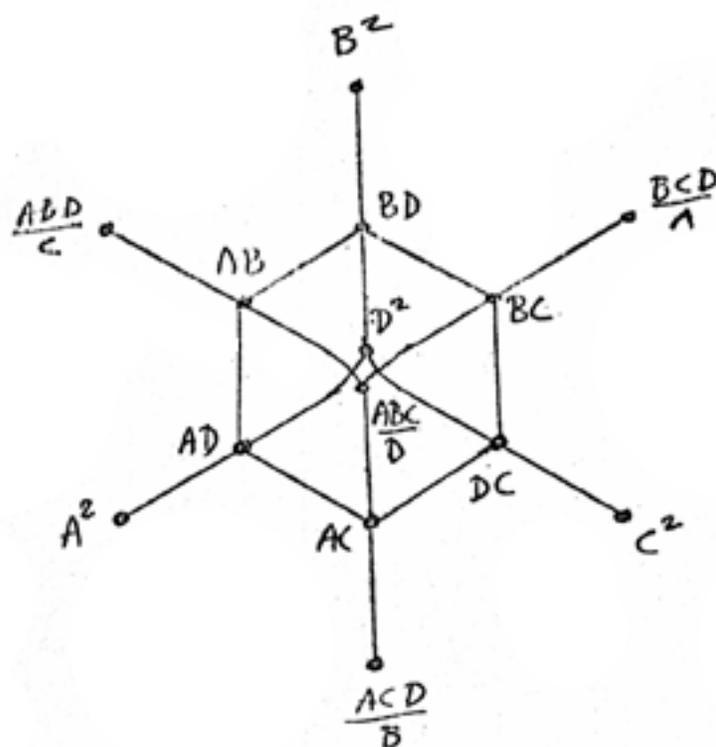
gold = 0) 4 increases
 black = 1) 4 tetragony
 red = 2) 4 hexagony
 green = 3) 4 tetragony
 purple = 4) 4 increases



(OVER)

(I'm using, here, an abbreviated lattice for drafting simplicity)

The 4 tetradic combinational series (and their 4 reciprocals, not shown) may be super-imposed on the 6 tones of the 2^4 hexany (in red) resulting in the figure I call mandala. Analogs to this figure exist in hexadic and ogdoadic, in all even-numbered orders of Tone-space.

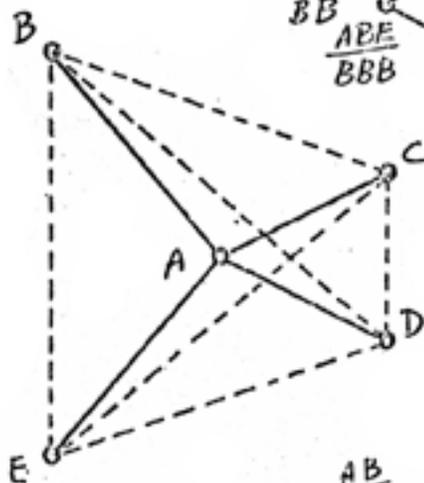
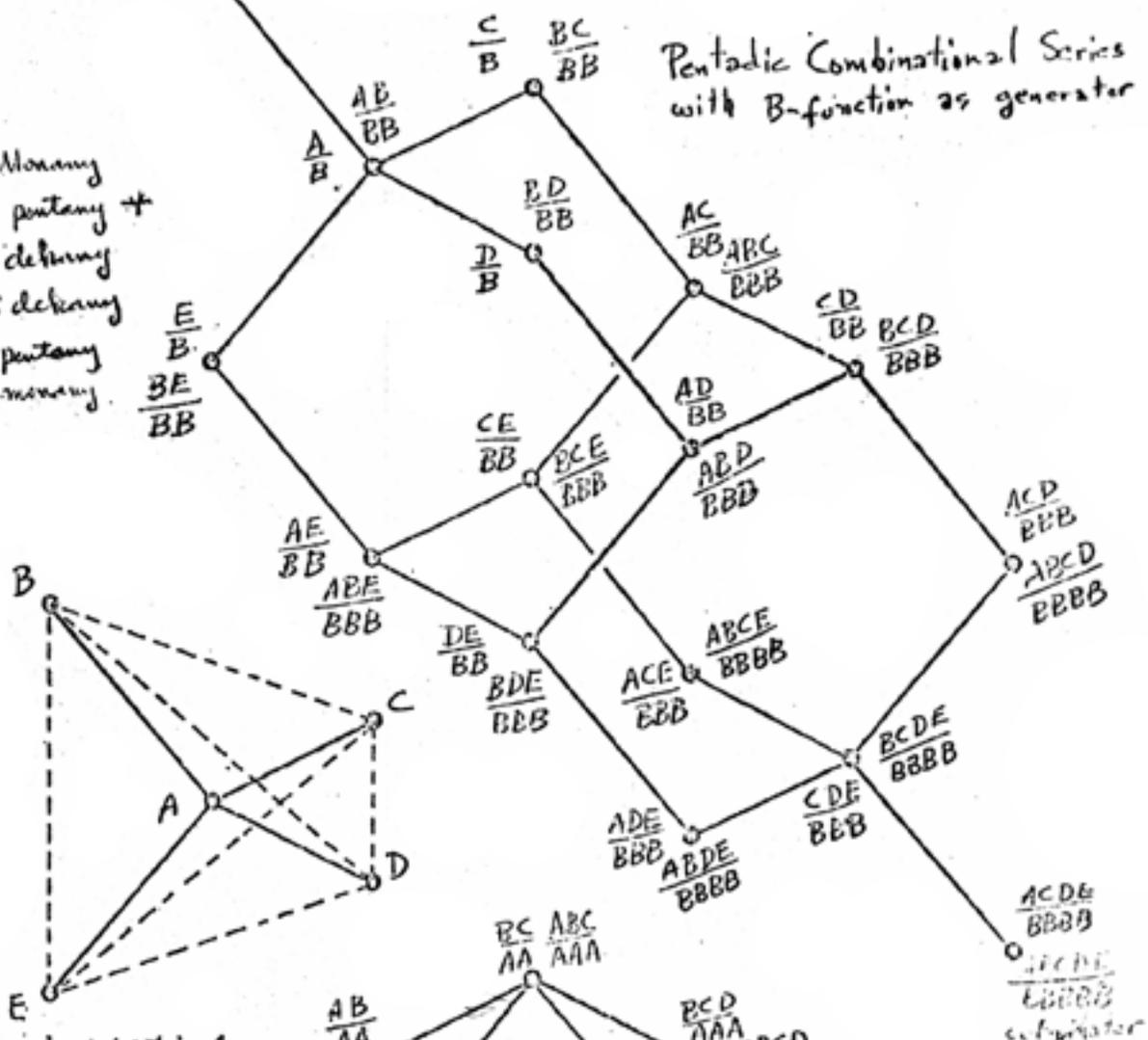


This figure is identical to its reciprocal, that is self-mirroring. The Tetrads progress in a "spherical" pattern, or, more specifically, in an octahedral pattern. (See separate sheet for complete lattice)

generator! $\frac{B}{B}$

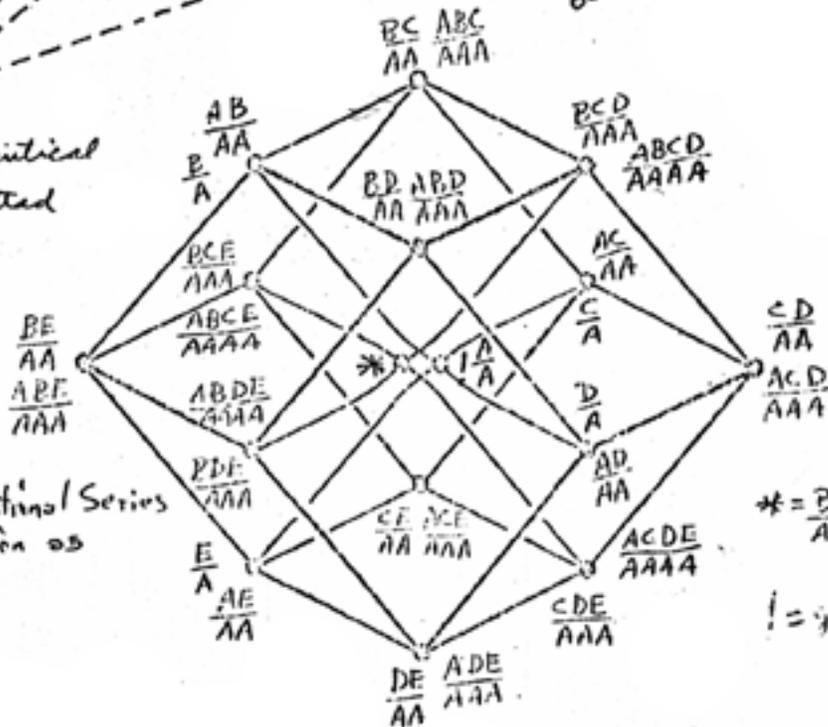
fold = 0) 5 Monamy
 black = 1) 5 pentamy +
 red = 2) 5 dekamy
 green = 3) 5 dekamy
 purple = 4) 5 pentamy
 orange = 5) 5 monamy

Pentadic Combinational Series
 with B-function as generator



* 1) 5 pentamy is identical
 to generating pentad

Pentadic Combinational Series
 with A-function as
 generator

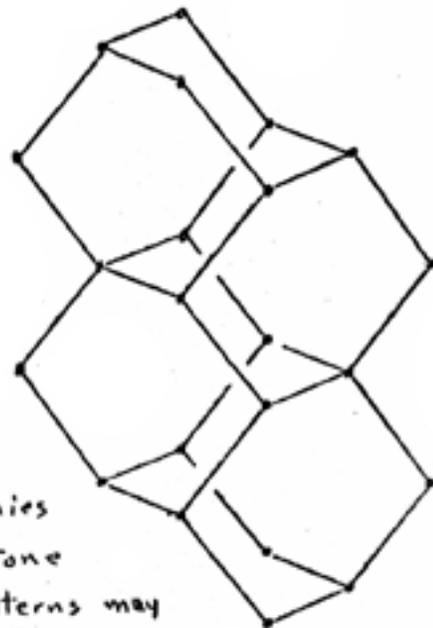
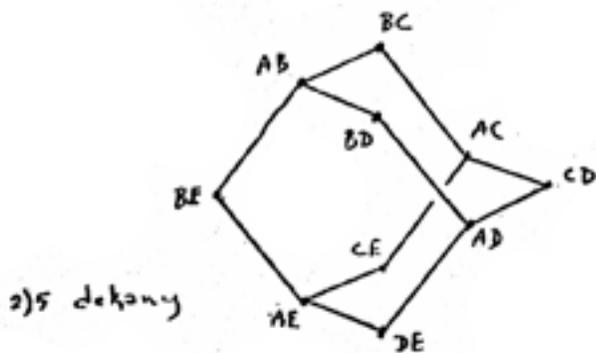


* = BCDE & generator
 ! = generator

(OVER)

This lattice is intended to be constructed and viewed in full-space. The generating module is an abbreviation of the centered-tetrahedron, using only the solid lines, from corners to center; as shown. When C, D, & E functions are used as generator (not shown) the results are structurally similar to the B-function generator (shown). Of extraordinary interest, to me, is the structure developed when the center of the centered-tetrahedron is taken as the generator (in this case the A-function, shown). This structure when seen in full space is the rhombic dodecahedron, plus dual centers at the generator & culminator. I had already used the 14-points of the dodecahedron as a nucleus for scale to development ^{long} before I observed its crystallographic implications.

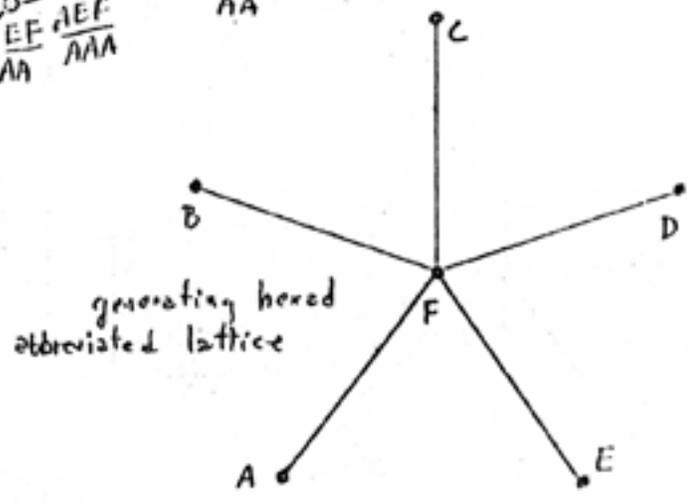
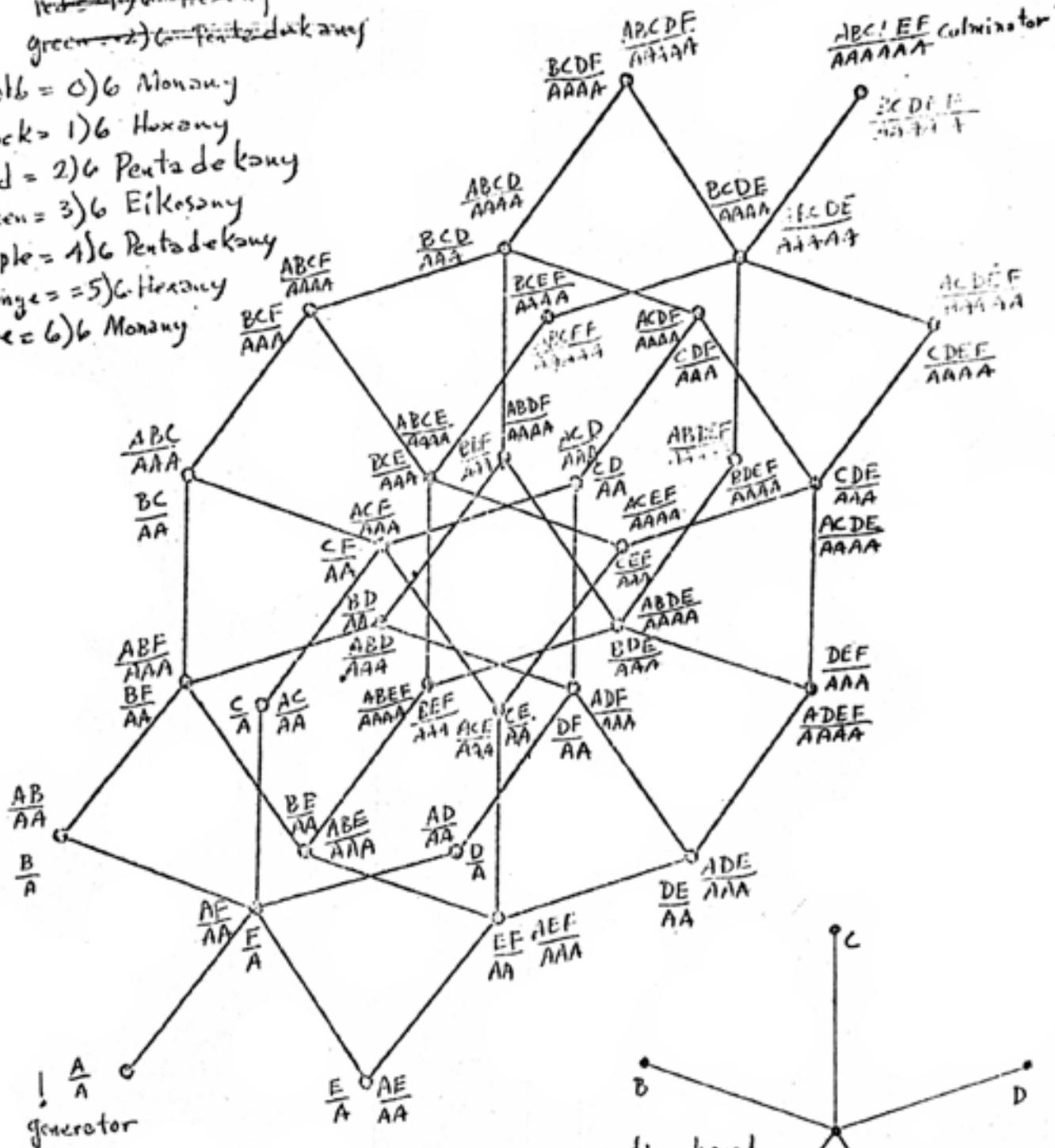
The 2)5 dekany, as can be observed, is this structure, which viewed in full space is visually most pleasing.



I have used this combination of dekany to construct a 22-tone structure. Such patterns may be extended indefinitely, to fill space.

Method of Constructing the Hexadic combinational series

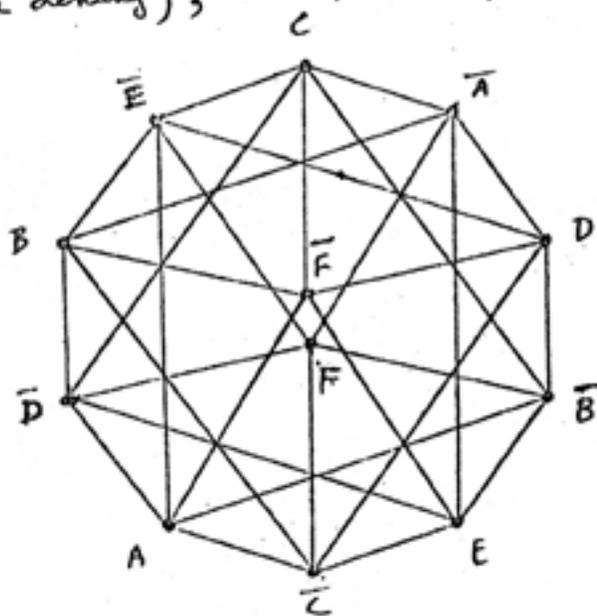
- gold = 0) 6 Monony
- black = 1) 6 Hexony
- Red = 2) 6 Pentadekany
- Green = 3) 6 Eikosany
- Purple = 4) 6 Pentadekany
- Orange = 5) 6 Hexony
- Blue = 6) 6 Monony



(OVER)

The Eikozany may be generated from each of the six functions of the hexad (A-function shown), and from each of the six functions of the reciprocal hexad.

On the flat the lattice yields a ten-fold symmetry. However, if one could view the Eikozany in hyper-space one would find a 12-fold symmetry (analogous to the eight facets or sides of the 2^4 Hexany) corresponding to the 12 possible generators. To illustrate, the Eikozany may be surrounded by 12 pentadekanies, each of which shares a dekaney in common with the Eikozany. In the diagram the points (=) signify a pentadekany (or a dekaney), identified by its immediate generator.



The ³⁰ connecting lines indicate ^{where} the pentadekanies (or dekanies) share a hexany in common.* This figure I call the heradic hypersphere; ^{and} it may be the basis for mirroring progressions. ^{Since} A perfectly regular hyperspherical progression is impossible in linear time, the hypersphere is meaningful, only, as a set of alternate possibilities.

*Also, the connecting lines, numbering 30, correspond to the number of hexanies in the eikozany.